

CS8625

Multistage interconnection networks
**CS8625 High Performance and
Parallel Computing**
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Class

Will

Start

Momentarily...

- Multi-stage interconnection networks: are a class of networks that provide a switched connection path.
- Switching buses are expensive, so a completely connected architecture is not scalable.
- So connections are made in a fixed pattern that uses multiple stages of switches.
- Transfers will go through multiple switches from source to destination.
- Multiple stages of switches take additional time (but it is small, due to the speed of the hardware).
- Not all combinations of connections are possible, due to conflicts at individual switches.

Dynamic and switched interconnection networks.

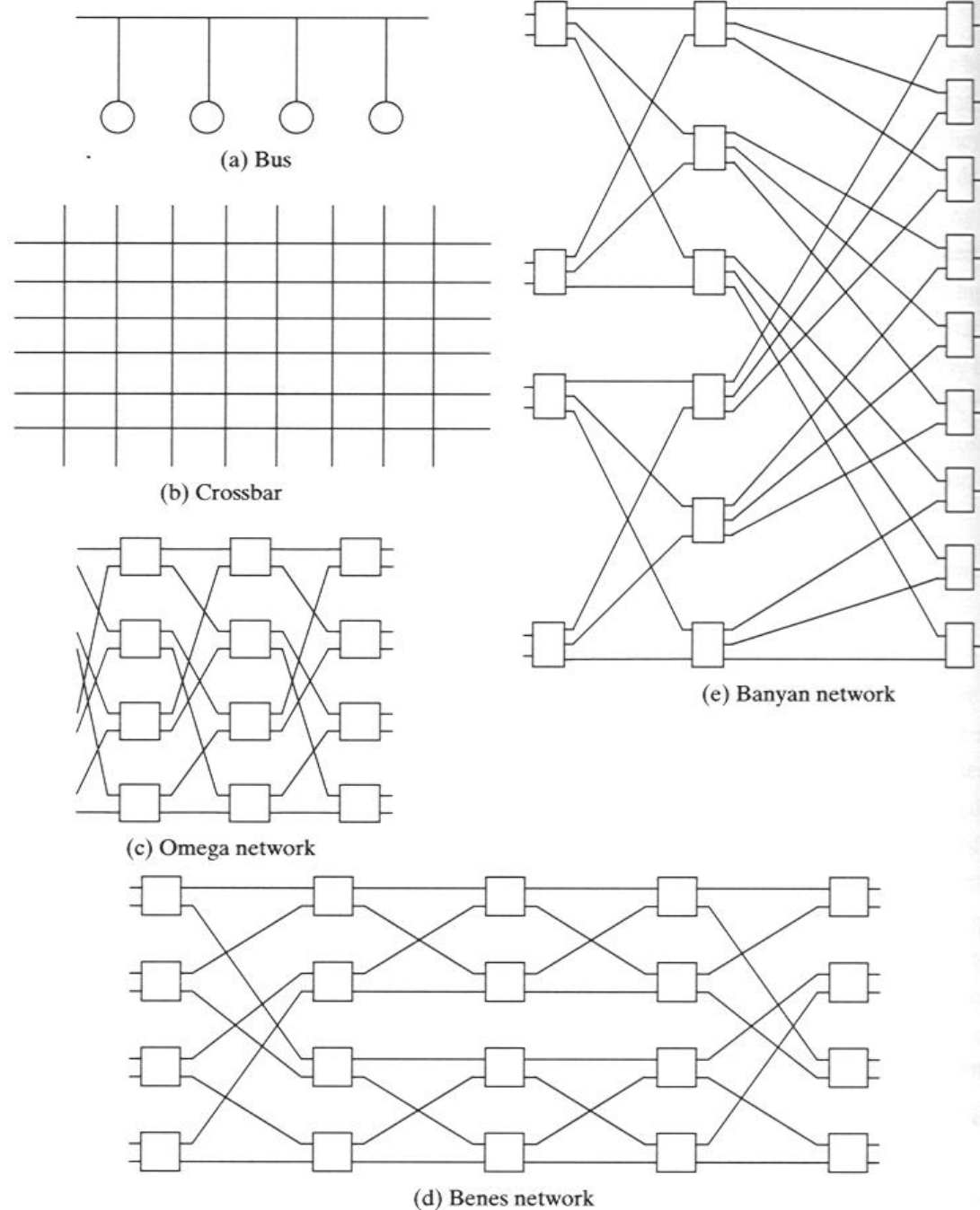
C,d,e, are multistage networks.

Cost of (a)? _____

Cost of (b) _____

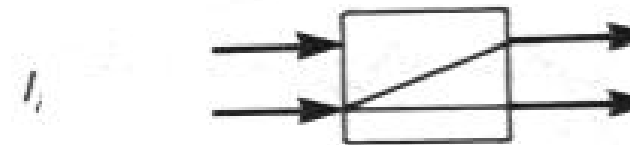
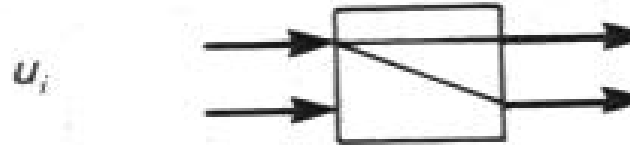
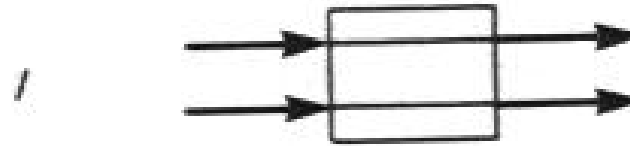
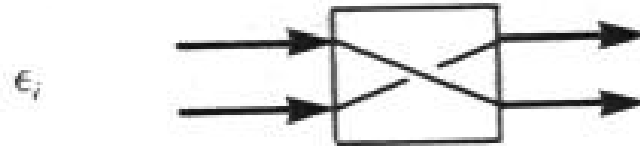
Cost of (c) _____

.



Coj

Figure 6-2 Dynamic interconnection networks.



X-bar switch too expensive.

Reduction (recursive) lowers cost.

Supports all $N!$ permutations of inputs onto outputs.

..at lower cost, and only slightly longer latency

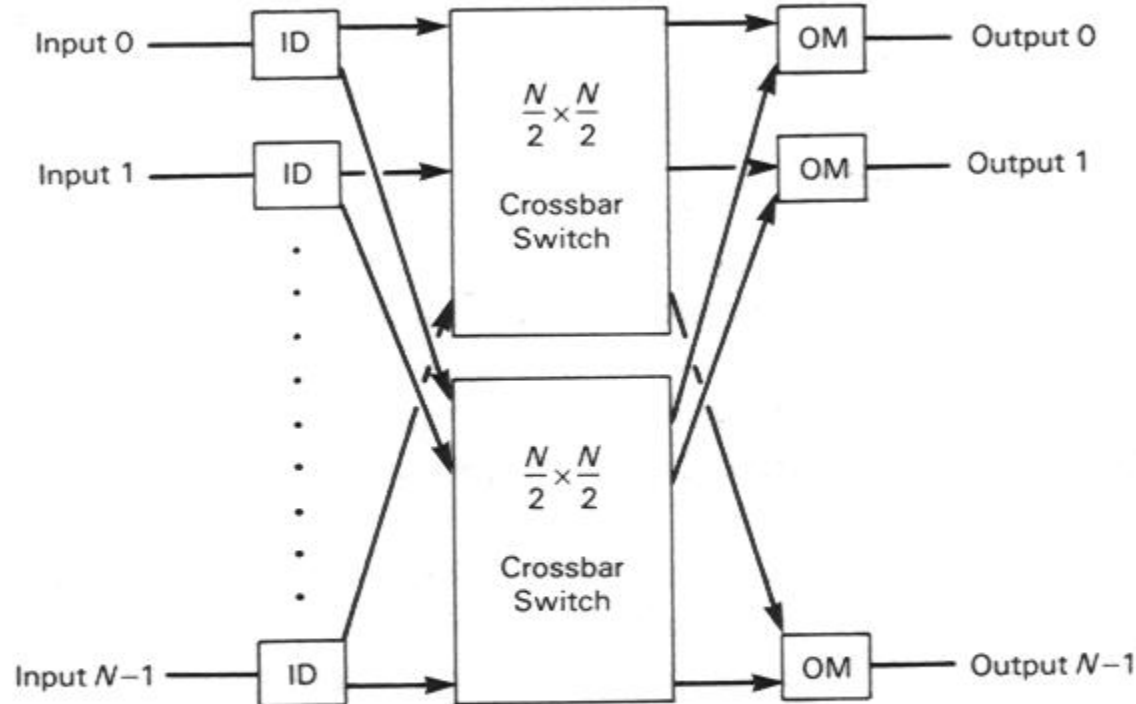


Figure 3.12 Beneš reduction of the cross-bar switch

Diagram ways
to map $0 \rightarrow 7$

Cost:

$$\frac{n}{2} [2 \log_2 N - 1]$$

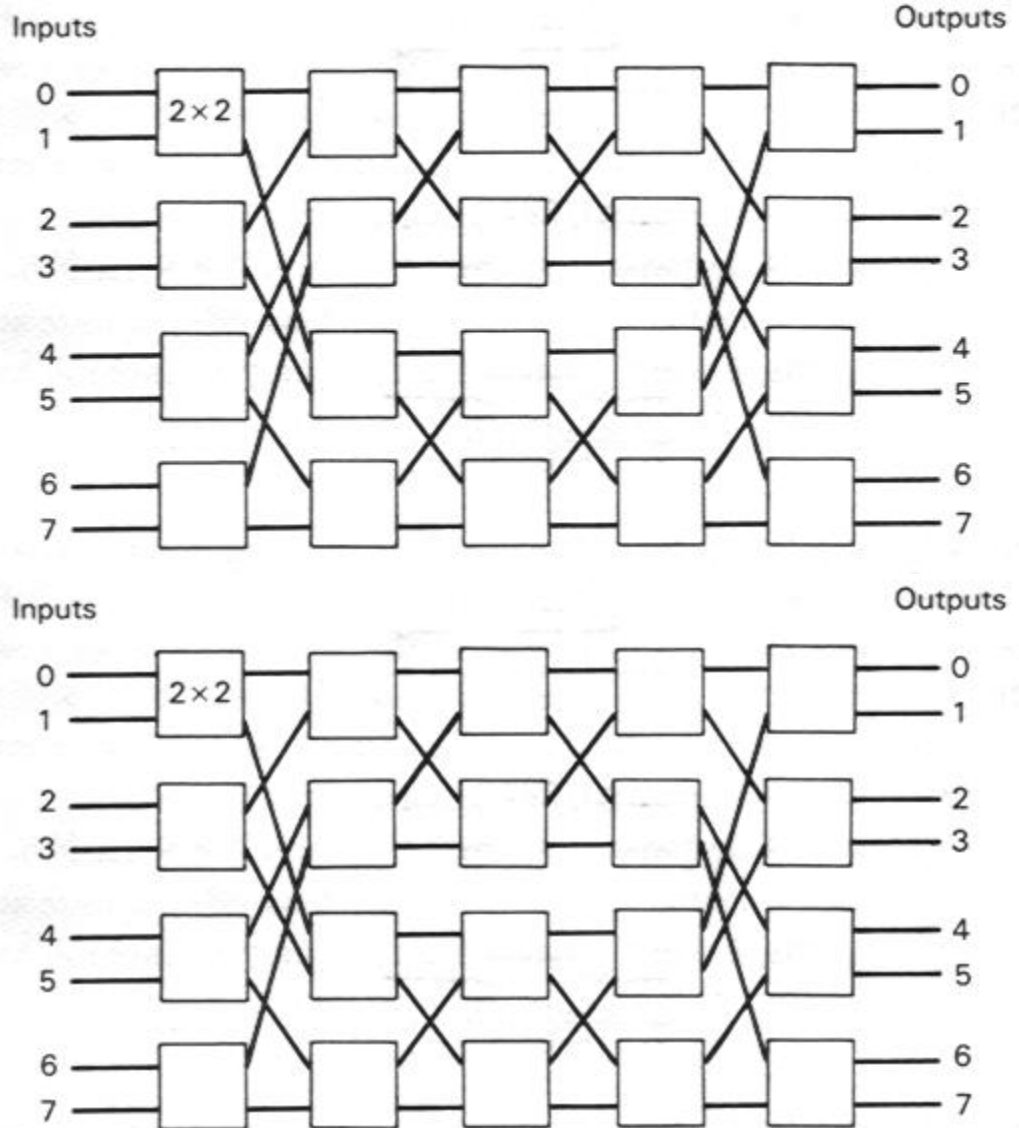


Figure 8.18 An 8-way Beneš network reduced to 2×2 cross-bar switches

- X-bar switch O_n^2
- Benes Network

$$\frac{n}{2} [2 \log_2 N - 1]$$

• N=	8	16	32	64	128
• Xbar:	64	256	1024	4096	16384
• Benes:	20	56	144	352	832

Test a
mapping:

0 → 7

1 → 5

2 → 4

3 → 0

4 → 1

5 → 6

6 → 3

7 → 2

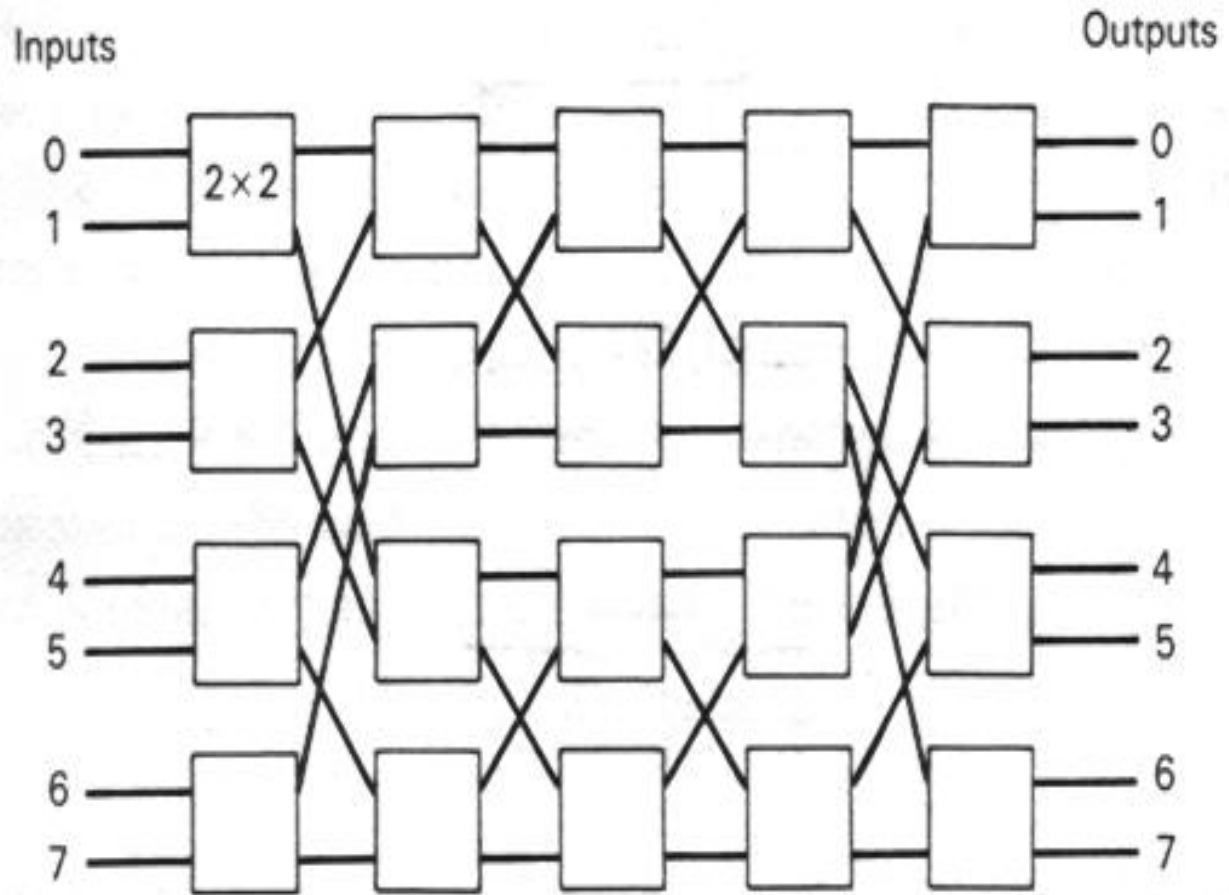


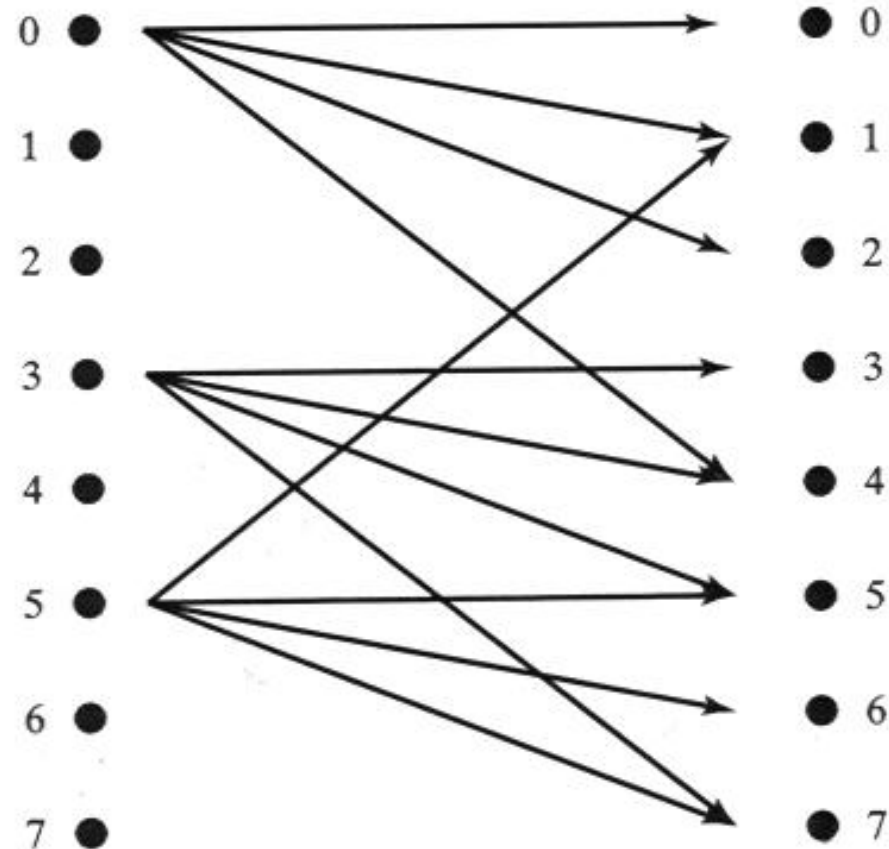
Figure 9.19 An 8-way Beneš network reduced to 2×2 cross-bar switches

- The design of the pattern of the switches is based on mathematics, that allows the switch settings to be described easily.
- Different settings of the switches (which define connections from source to destination) represent different “permutations”, which can be mathematically described.

Cyclic shifts of 2^h places for $0 \leq h < m$, where $N = 2^m$, can be done with $M \log_2 N$ switches and $\log_2 N$ control signals. Each source, S , has m switches connecting it to destinations, $(S + 2^h) \bmod N$, for $0 \leq h < m$, see Figure 6-3. To maintain a readable diagram, output connections are only shown for nodes 0, 3, and 5. A shift of any length from 1 to N can be done by $\log_2 N$ or fewer of these shifts. The set of permutations for different values of h constitutes the m -dimensional hypercube routing functions that are supported by the hypercube networks.

For instance, connections at node 3 are :

If data at 3, needs to get to 1?



**End
Of
Today's
Lecture.**

